

# Forecasting drought revisited – the importance of spectral transformations to dominant atmospheric predictor variables

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## Water Resources Research

Technical Reports: Methods

### Refining Predictor Spectral Representation Using Wavelet Theory for Improved Natural System Modeling

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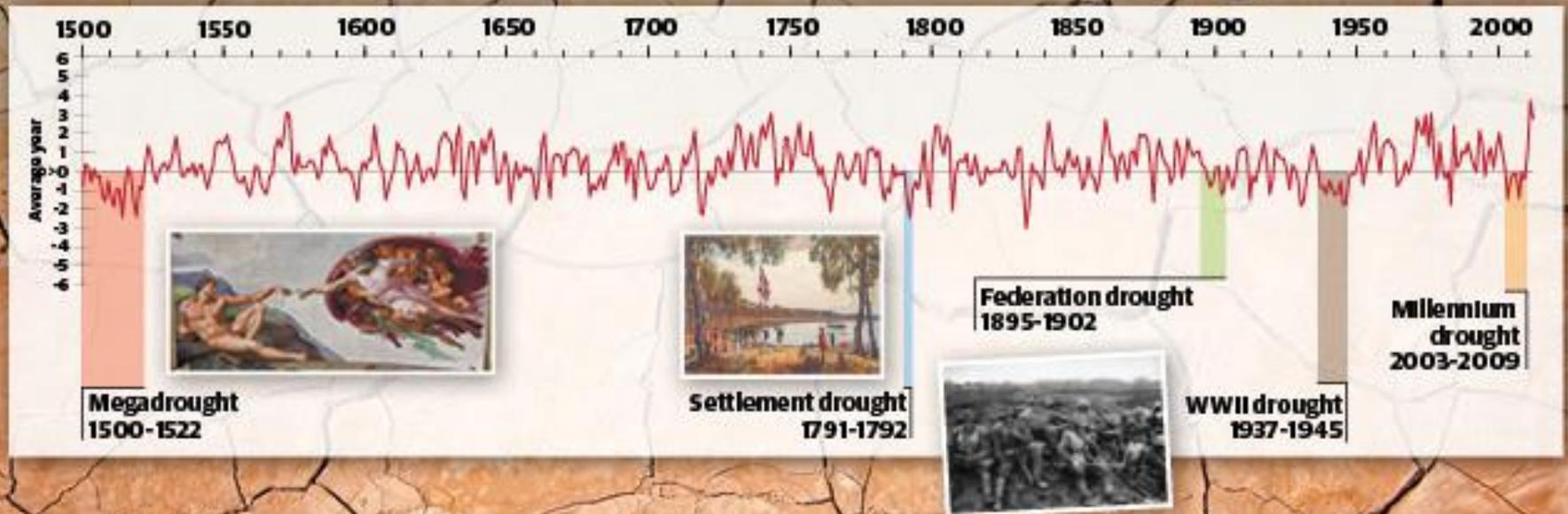


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# DRY VIEW OF HISTORY

## Drought Severity Index for South East Australia



Source: Australian Institute of Marine Science

# Forecasting basics revisited

1. Should predictor variables be transformed to mimic the probability distribution of the response?

**ANS – Yes, especially for linear models where log or Box-Cox transforms are often used**

2. Should predictor variable be required to exhibit similar spectral attributes as the response?

**ANS – Ideally yes, as they will have similar persistence attributes as the response**

3. HOW?

**ANS – Using a suitable Fourier or Wavelet transformation**

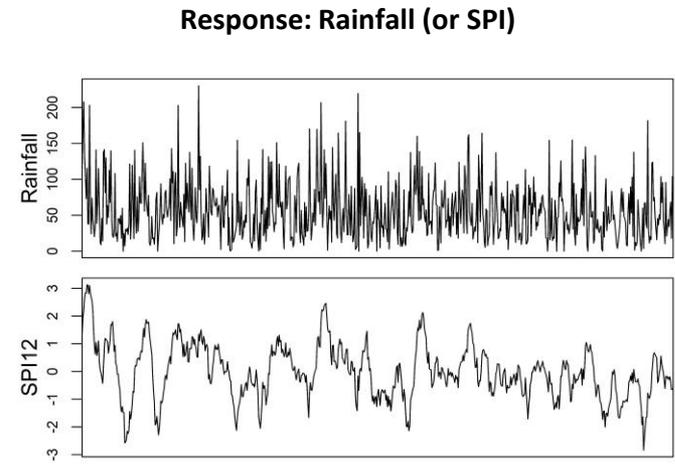
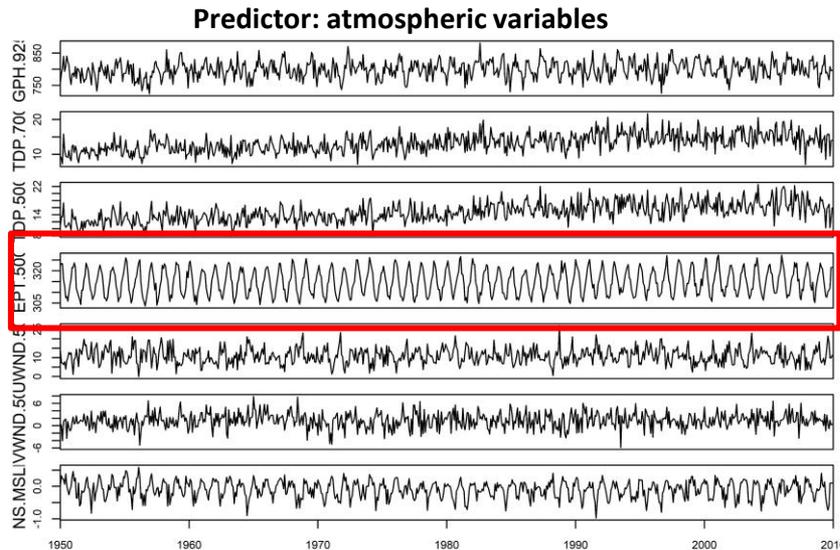
**PROBLEM – Need to know “future” values of the predictor – only possible when the predictors are being simulated using a model (such as a General Circulation Model)**

**THIS MAY BE OUR BEST OPTION FOR PREDICTING DROUGHT INTO THE FUTURE!**

# How to refine predictor variable to improve modelling?

The hypothesis:

If the spectrum of the predictor is similar to response, the predictive model exhibits better accuracy than otherwise.



# How to modify the spectrum?

Background: Wavelet Transform

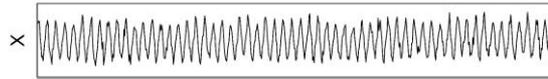
**Additive Decomposition:**  
(Multiresolution Analysis, MRA)

$$X = \sum_{j=1}^J d_j + a_J$$

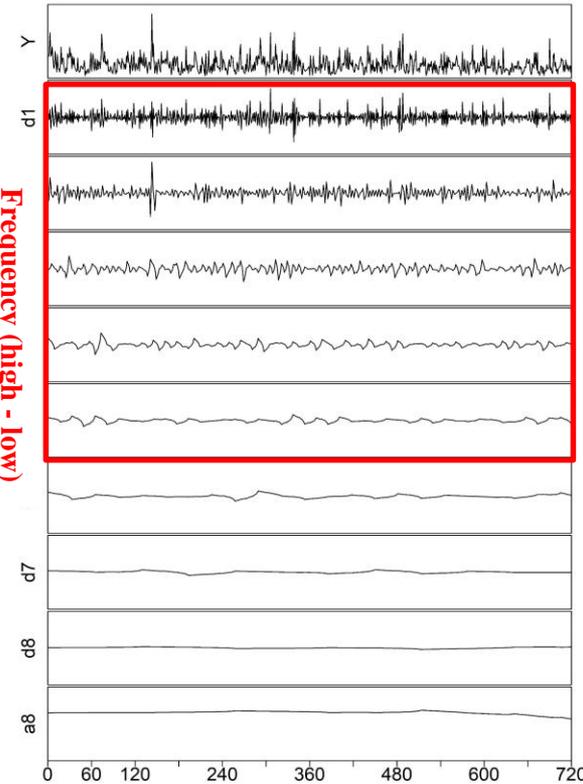
$$\sigma_X^2 = \sum_{j=1}^J \sigma_{d_j}^2 + \sigma_{a_J}^2$$

- Remarkably different spectrum properties
- Our target: variance-transformed predictor

Predictor Variable X (EPT)



Target Response Y (Rainfall)



# How to modify the spectrum to optimise predictability?

**Change predictor  $X$  to  $X'$  such that  $X'$  has a closer spectral representation to the response  $Y$**

**MRA:**

$$X = \sum_{j=1}^J d_j + a_J$$
$$\sigma_X^2 = \sum_{j=1}^J \sigma_{d_j}^2 + \sigma_{a_J}^2$$

**Matrix form:**

$$X = \tilde{R}I$$

where  $\tilde{R}$  is standardized reconstructions matrix.

$$R = [d_1, \dots, d_J, a_J] \quad I = [\sigma_{d_1}, \dots, \sigma_{d_J}, \sigma_{a_J}]^T$$

**What we are looking for:**

$$X' = \tilde{R}\alpha$$

$$\alpha = \sigma_X \tilde{C}$$

where  $\tilde{C}$  is the normalized covariance matrix for the variable set  $(Y, \tilde{R})$

$$C = \frac{1}{n-1} Y^T \tilde{R} = [S_{Y\tilde{d}_1}, \dots, S_{Y\tilde{d}_J}, S_{Y\tilde{a}_J}]$$

$$RMSE_{\min} = \sqrt{\frac{n-1}{n} (\sigma_Y^2 - \|C\|^2)}$$

# Results – Synthetic example

A dynamic example (Rössler system):

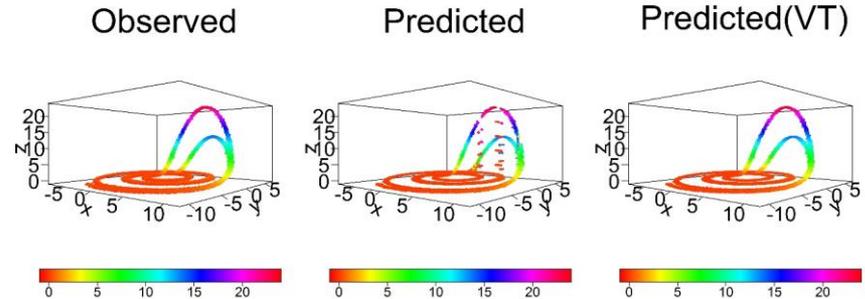
$$\begin{aligned}\dot{x} &= -y - z, \\ \dot{y} &= x + ay, \\ \dot{z} &= b + z(x - c).\end{aligned}$$

Use  $x$  and  $y$  to predict  $z$

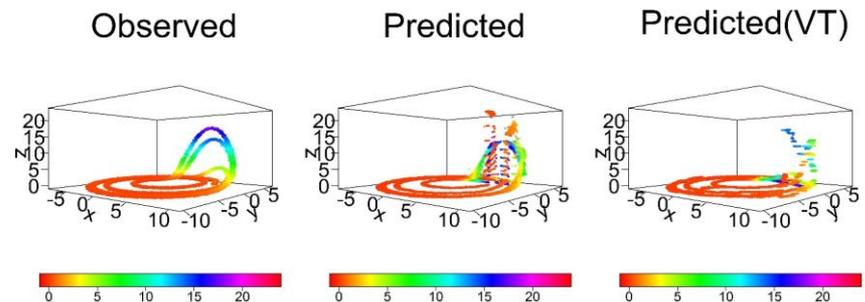
**Predicted:** predicted  $z$  using original  $x$  and  $y$

**Predicted (VT):** predicted  $z$  using variance-transformed  $x$  and  $y$

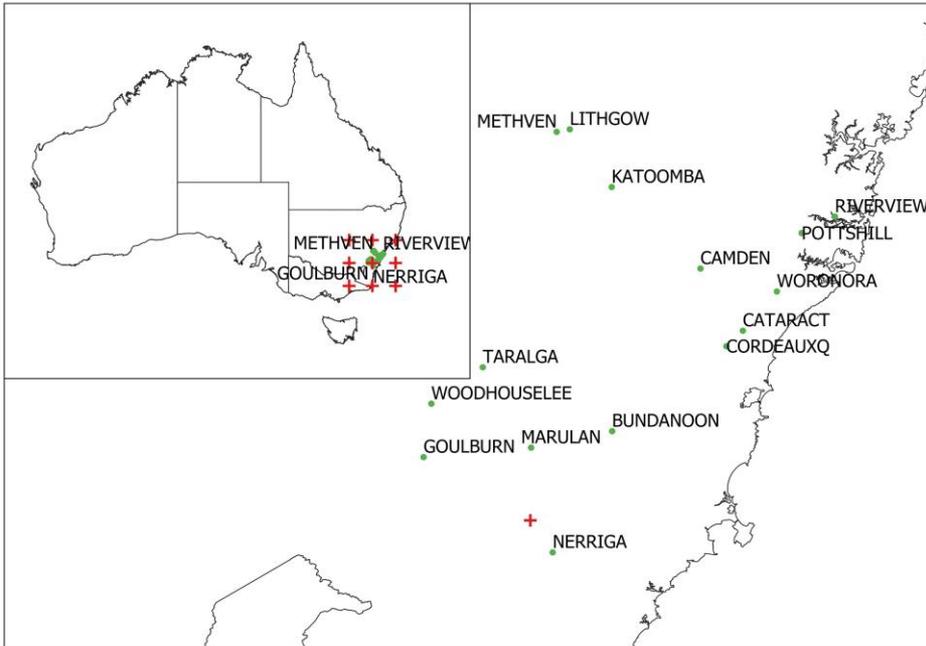
**Calibration:** RMSE = 0.113 against 1.189



**Validation:** RMSE = 2.550 against 4.493



# Results – Real example



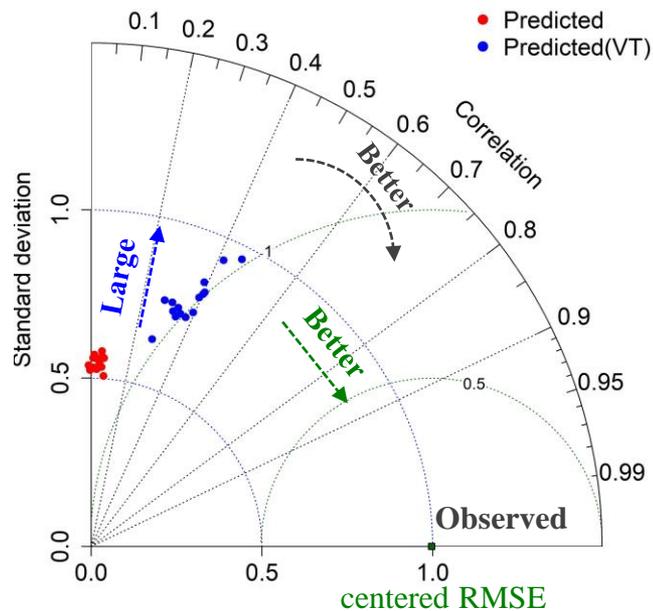
- Sydney Region Rainfall Stations
- ✚ NCEP-NCAR Reanalysis Grids

**Target response: Drought Index (SPI12, 1950 – 2009)**

Predictor No.	Predictor Name
1	Geopotential heights (m) at 925 hPa (GPH@925)
2	Temperature depression (degree C) at 700 hPa (TDP@700)
3	Temperature depression (degree C) at 500 hPa (TDP@500)
4	Equivalent potential temperature (Kelvin K) at 500 hPa (EPT@500)
5	Zonal Wind (m/s) at 500 hPa (UWND@500)
6	Meridional Wind (m/s) at 500 hPa (VWND@500)
7	N-S gradient of mean sea level pressure (NS-MSLP)

# Results – Real example

**Predicted: Original predictors**  
**Predicted (VT): Variance-transformed predictors**



Taylor diagram evaluating model performance by the standard deviation, centered RMSE and correlation coefficient.

# To wrap up....

- A **unique** variance transformation is identified for each predictor variable that explains **maximal** information in the corresponding response.
- Results of a dynamic example and a real application show **clear improvements in predictability** compared to the use of untransformed predictors.
- It is a **generic** method and not limited to hydro-climatological systems.
- Application to **correct** GCM drought projections using this approach are underway

## Future Work:

- The variance transformation technique for forecast with no dependence on future data
- The variance transformation technique for multivariate response characterization

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